

Yoneda's Isomorphism Commutes with Homology

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Let C be a chain complex in an abelian category \mathcal{A} , and let $T: \mathcal{A} \rightarrow \mathcal{A}b$ be a right exact functor into the category of abelian groups. Then there is an isomorphism, the homological Yoneda isomorphism,

$$\text{Nat}(H^n \text{Hom}_{\mathcal{A}}(C, -), T) \xrightarrow{\cong} H_n TC$$

which is natural in C and in T . – We will prove this result and present some immediate consequences. Then we extend the homological Yoneda isomorphism to functors $T: \mathcal{X} \rightarrow \mathcal{A}b$, where \mathcal{X} is a semiabelian category, and T is a right exact functor. An application to the topic of ‘universal n -fold central extensions’ in a semiabelian variety concludes the talk.